Mathematical Models

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Investment In Smart Homes Consumer And Distributor Perspectives

Seyyedreza Madani

joint work with Pierre-Olivier Pineau

June 7, 2021



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Rational behind V2G



Figure 1: Generation and load in a sample week in March

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Smart Home Management



Figure 2: dcbel device

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Image: A matrix

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Previous studies

• The influences of Vehicle to Grid (V2G) system and its integration with RESs on the environment, society and economy [BTM21]

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Previous studies

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- The influences of Vehicle to Grid (V2G) system and its integration with RESs on the environment, society and economy [BTM21]
- Ownership challenge: Aggregators and Other Actors in the market [NZdRKS19]

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- Profitability of V2H [LP20]

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- Ownership challenge: Aggregators and Other Actors in the market [NZdRKS19]
- Profitability of V2H [LP20]
- Premium tariff rates for V2G [Ric13]

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- The influences of Vehicle to Grid (V2G) system and its integration with RESs on the environment, society and economy [BTM21]
- Ownership challenge: Aggregators and Other Actors in the market [NZdRKS19]
- Profitability of V2H [LP20]
- Premium tariff rates for V2G [Ric13]
- Some case studies on the profitability of V2G: in the Netherlands [vdV20], China [LTL⁺20] and, India [LAAP⁺21]

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Investment Scenarios

Scenario	Capacity of the stationary battery (kWh)	Capacity of the EV's battery (kWh)	Solar PV availability	Total cost (purchase and installation, USD)
0 – Status quo	×	×	×	0
1 – Battery	40.5	×	×	27,300
2 – Battery + PV	27	×	Yes	35,125
3 – EV	×	36	×	4,000
4 - EV + PV	×	36	Yes	17,145
5 – Battery + EV + PV	10	36	Yes	23,724

Investment cost of the scenarios



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Main problems

• Which agent? Profitability of investment in smart home for the distributor and the prosumer

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Main problems

- Which agent? Profitability of investment in smart home for the distributor and the prosumer
- Which scenario? The best investment scenario for smart home technologies

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Main problems

- Which agent? Profitability of investment in smart home for the distributor and the prosumer
- Which scenario? The best investment scenario for smart home technologies
- Which rate? Effects of different tariff structures on profitability of smart home technologies

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Main problems

- Which agent? Profitability of investment in smart home for the distributor and the prosumer
- Which scenario? The best investment scenario for smart home technologies
- Which rate? Effects of different tariff structures on profitability of smart home technologies
- Consequences? Effects of different scenarios on the annual cost and monthly peak-loads

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Assumptions

• All parameters are deterministic and given in the beginning

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- All parameters are deterministic and given in the beginning
- Real consumption and generation records are used (provided by the Green Mountain Power (GMP) distribution company in Vermont)

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- All parameters are deterministic and given in the beginning
- Real consumption and generation records are used (provided by the Green Mountain Power (GMP) distribution company in Vermont)
- The same charge/discharge limitation and efficiency rates are used for battery and EV

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Conclusion

- All parameters are deterministic and given in the beginning
- Real consumption and generation records are used (provided by the Green Mountain Power (GMP) distribution company in Vermont)
- The same charge/discharge limitation and efficiency rates are used for battery and EV
- In GMP's model, Real-Time Locational Marginal Price (RTLMP) (\$/kWh) in Vermont is used. The buying and selling prices are equal.

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In prosumer model, five tariff structures are used:

Rate Name	Fixed charge		Rate
	(\$/day)		(\$/kWh)
Flat (FX)	0.492	Usage	0.16859
Time-of-Use	0.651	Peak-Load Usage	0.26771
(TOU)		Off-Peak Usage	0.11411
FX for home &	0.651	General Usage	0.16859
TOU for EV		Off-Peak EV Usage	0.12831
RTLMP	0	price updates every	5 minutes
Buying at TOU	0.651	Peak-Load Usage	0.26771
from grid &		Off-Peak Usage	0.11411
Selling at RTLMP		price updates every	5 minutes
back to grid			

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$t \in \{\mathcal{T}\}$ episode t in horizon $[1, 2, 3, \dots, T]$ $k \in \{\mathcal{K}\}$ month k in horizon $[1, 2, 3, \dots, K]$

• A full year (8,760 hours) with 15 minutes time-steps (t) is considered here.¹

¹Note that when 1 kWh is used during this time interval means that 4 kW of power/capacity are being used **HEC** Montreal

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	$B^{max} = capacity (kWh) of battery$	=
	$B^{min} =$ minimum allowed electricity (kWh) in battery	=
	E^{max} = capacity (kWh) of EV	=
	$E^{min} =$ minimum allowed electricity (kWh) in EV	=
	$U^c={ m charging\ capacity\ (kWh)\ of\ battery/EV\ during\ the\ interval}$	-
	$U^d = discharging capacity (kWh) of battery/EV during the interval$	=
1	$1 - \eta^{c} = charging loss rate$	=
1	$1-\eta^d={\sf discharging\ loss\ rate}$	=

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Parameters cntd.

$$P^{rns} = \text{cost coefficient ($/kW) of RNS}$$

$$P^{cap} = \text{cost coefficient ($/kW) of capacity}$$

$$P_t^{buy} =$$
 electricity price ($\frac{1}{k}$) to buy from grid at time t

$$P_t^{sell} =$$
 electricity price (\$/kWh) to sell to grid at time t

$$L_t = \text{load (kWh) at time } t$$

$$A_t$$
 = availability of EV at time t under the chosen scenario

$$V_t = {\sf EV}$$
 usage (kWh) (for vehicle riding) at time t under the chosen so

$$R_t$$
 = electricity generation (kWh) from solar panel t

$$I^{trade}$$
 = indicates if it is allowed to sell electricity to grid

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Decision Variables

 x_t^{GL} = electricity (kWh) from grid to load at time t x_t^{GB} = electricity (kWh) from grid to battery at time t x_t^{GE} = electricity (kWh) from grid to EV at time t x_t^{RL} = electricity (kWh) from solar panel to load at time t x_t^{RB} = electricity (kWh) from solar panel to battery at time t x_t^{RE} = electricity (kWh) from solar panel to EV at time t x_t^{RE} = electricity (kWh) from solar panel to EV at time t

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Decision Variables cntd.

$$x_t^{BL}$$
 = electricity (kWh) from battery to load at time t
 x_t^{EL} = electricity (kWh) from EV to load at time t
 x_t^{BG} = electricity (kWh) from battery to grid at time t
 x_t^{EG} = electricity (kWh) from EV to grid at time t
 x_k^{peak} = maximum electricity (kWh) taken from grid in an episode in more

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State variables

 b_t^B = available electricity (kWh) in stationary battery at time t b_t^E = available electricity (kWh) in EV battery at time t

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Distributor's Model I

objective function

$$\min \sum_{t=1}^{T} \left(P_t^{buy}(x_t^{GL} + x_t^{GB} + x_t^{GE}) \right)$$
 buying cost
$$- P_t^{sell}(x_t^{RG} + \eta^d x_t^{BG} + \eta^d x_t^{EG}))$$
 selling revenue
$$+ 4 \sum_{k=1}^{12} \left(P^{rns} + 1.35P^{cap} \right) x_k^{peak}$$
 network charge (1)

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Distributor's Model II

Subject to:

Covering load

$x_t^{GL} + \eta^d (x_t^{BL} + x_t^{EL}) + x_t^{RL} \ge L_t \qquad \forall t \qquad (2)$

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Distributor's Model III

availability of EV and stored energy limitation

$$x_t^{BL} + x_t^{BG} \le b_t^B \qquad \qquad \forall t \qquad (3)$$

$$x_t^{EL} + x_t^{EG} \le b_t^E A_t \qquad \qquad \forall t \qquad (4)$$

$$x_t^{GE} + x_t^{RE} \le E^{max} A_t \qquad \qquad \forall t \qquad (5)$$

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Distributor's Model IV

charging and discharging limits

$$x_t^{BL} + x_t^{EL} + x_t^{BG} + x_t^{EG} \le U^d \qquad \forall t \qquad (6)$$

$$x_t^{GB} + x_t^{GE} + x_t^{RB} + x_t^{RE} \le U^c \qquad \forall t \qquad (7)$$

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Distributor's Model V

stored energy limitations

$$B^{min} \le b_t^B \le B^{max} \qquad \forall t \qquad (8)$$
$$E^{min} \le b_t^E \le E^{max} \qquad \forall t \qquad (9)$$

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Distributor's Model VI

PV generation

$$x_t^{RL} + x_t^{RB} + x_t^{RE} + x_t^{RG} \le R_t \qquad \forall t \qquad (10)$$

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Distributor's Model VII

State transition

$$b_t^B + \eta^c (x_t^{GB} + x_t^{RB}) - (x_t^{BL} + x_t^{BG}) = b_{t+1}^B \forall t$$
(11)
$$b_t^E + \eta^c (x_t^{GE} + x_t^{RE}) - (x_t^{EL} + x_t^{EG}) - \frac{V_t}{\eta^d} = b_{t+1}^E \forall t$$
(12)

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Distributor's Model VIII

peak load calculation

$$x_t^{GL} + x_t^{GB} + x_t^{GE} \le x_k^{peak} \forall t \in k, k$$
(13)

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Distributor's Model IX

domain of the decision variables

$$\begin{array}{l} x_{t}^{RL}, x_{t}^{RB}, x_{t}^{RE}, x_{t}^{RG}, x_{t}^{BG}, x_{t}^{EG}, x_{t}^{BL}, \\ x_{t}^{EL}, x_{t}^{GL}, x_{t}^{GB}, x_{t}^{GE}, x_{k}^{Peak}, b_{t}^{B}, b_{t}^{E} \ge 0 \end{array} \qquad \forall t \qquad (14)$$

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Prosumer's Model I

objective function

$$\min \sum_{t=1}^{T} \left(P_t^{buy} (x_t^{GL} + x_t^{GB} + x_t^{GE}) - P_t^{sell} (x_t^{RG} + \eta^d x_t^{BG} + \eta^d x_t^{EG}) \right)$$
(15)

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Prosumer's Model II

Subject to: Constraints 2 to 12

Trade allowance

$$x_t^{RG} + x_t^{BG} + x_t^{EG} \le (U^d + R_t)I^{trade} \qquad \forall t \qquad (16)$$

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Prosumer's Model III

domain of the decision variables

$$\begin{array}{l} x_{t}^{RL}, x_{t}^{RB}, x_{t}^{RE}, x_{t}^{RG}, x_{t}^{BG}, x_{t}^{EG}, x_{t}^{BL}, \\ x_{t}^{EL}, x_{t}^{GL}, x_{t}^{GB}, x_{t}^{GE}, b_{t}^{B}, b_{t}^{E} \geq 0 \end{array} \qquad \forall t \qquad (17)$$

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Image: A matrix

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GMP invests and controls Prosumer invests and controls

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Conclusion

NPV of scenarios when system is controlled by GMP



• Scenario #3 (having only EV) is the only profitable (+\$909.3) investment scheme for the distributor. (i = 0.0619, N = 15)

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Conclusion

Peak-Loads when GMP controls the system



Peak-load shaving under different investment scenarios

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NPV of scenarios when system is controlled by PRO

V2H, selling back to grid is NOT allowed



• All scenarios under any rate structure yield negative NPVs.

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NPV of scenarios when system is controlled by PRO

V2G, selling back to grid is allowed



- RTLMP and TOU&RTLMP rate structures make any investment scenario UNPROFITABLE.
- S1 (Battery) and S2 (Battery+PV) are always UNPROFITABLE.

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GMP's cost when system is controlled by PRO

V2G, selling back to grid is allowed



 Choosing Time-Of-Use-EV&Flat yields the least cost for GMP, regardless of the PRO's investment scenario.

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Peak-Loads when system is controlled by PRO (selling is allowed)

Peak loads when system is controlled by PRO (Rate: Time-of-Use)



Peak loads when system is controlled by (Rate: Time-of-Use EV & flat)



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Flow from Grid when system is controlled by PRO (in 15-minutes time-steps)

rate is TOU-for-EV-and-FX and selling back to grid is allowed



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Who should invest?

- The optimal investment strategy for the distributor's investment returns the NPV of \$909.32
- The optimal investment strategy for the prosumer's investment returns the NPV of up to \$11,728.92 (under proper tariff structure)
- A proper investment by the prosumer can save in both prosumer's and distributor's yearly costs.

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What investment scenario to choose?

- The one and only profitable investment scenario for the distributor is scenario #3 (EV)
- (Under proper tariff structure) the best investment scenarios for the prosumer are scenario #4 (EV+PV), scenario #3 (EV), and, scenario #5 (Battery+EV+PV), respectively.

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What tariff to impose?

- If selling back to grid is NOT allowed (v2H), all investment scenarios are UNPROFITABLE
- investment made by the prosumer usually increases the distributor's costs, however, TOU-for-EV&FX cuts the yearly costs of both agents.

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Future works

- Developing a dynamic model with uncertain parameters
- Investigating collective investment scenarios (allowing local sharing)
- Considering effects of mass smart home technology adaption consequences on loads and prices

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References

[BTM21]	Bijan Bibak and Hatice Tekiner-MoħulkoÄğ. A comprehensive analysis of vehicle to grid (v2g) systems and scholarly literature on the application of such systems. <i>Renewable Energy Focus</i> , 36:1–20, 2021.
[LAAP ⁺ 21]	K. Logavani, A. Ambikapathy, G. Arun Prasad, Ahmad Faraz, and Himanshu singh. Smart Grid, V2G and Renewable Integration, pages 175–186. Springer Singapore, Singapore, 2021.
[LP20]	JosĂle-Lise Leheutre and Pierre-Olivier Pineau. Profitability of a vehicle-to-home system in different electricity tariff contexts. Rapport dâĂZĂl'tude de la Chaire de gestion du secteur de lâĂZĂl'nergie, 03, 2020.
[LTL ⁺ 20]	Xinzhou Li, Yitong Tan, Xinxin Liu, Qiangqiang Liao, Bo Sun, Guangyu Cao, Cheng Li, Xiu Yang, and Zhiqin Wang. A cost-benefit analysis of v2g electric vehicles supporting peak shaving in shanghai. <i>Electric Power Systems Research</i> , 179:106058, 2020.
[NZdRKS19]	Lance Noel, Gerardo Zarazua de Rubens, Johannes Kester, and Benjamin K. Sovacool. <i>The Economic and Business Challenges to V2G</i> , pages 91–116. Springer International Publishing, Cham, 2019.
[Ric13]	David B. Richardson. Encouraging vehicle-to-grid (v2g) participation through premium tariff rates. Journal of Power Sources, 243:219–224, 2013.
[vdV20]	MT van der Ven. Vehicle to grid in utrecht: Integrating electric vehicles into the energy system of utrecht. Master's thesis, 2020.

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